## $\begin{array}{llllll}7 & 8 & 9 & 10 & 11 & 12\end{array}$



TI-Nspire CAS


Investigation


Student

## Aim

To compare the height, weight, age and field positions of all football players from the 32 teams which participated in the 2010 FIFA World Cup in South Africa.

National Curriculum Statement: Determine quartiles and interquartile range (ACMSP248).

ScOT: Inter-quartile range

## Equipment

For this activity you will need:

- TI-Nspire CAS
- TI-Nspire CAS file: FIFA World Cup 2010

Students can use digital technologies to compare various attributes of the participating teams in the 2010 FIFA World Cup.

## Problem Description

The data consists of 32 teams and each team contains 23 players. Data includes country of origin, allocated group (A, B, C, D, E, F, G and H) player's position (forward, midfielder, defender and goalkeeper), weight in kilograms, height in centimetres and age in years. The data is contained in Lists \& Spreadsheet page.

## Technology

During this activity, students will need to use the TI-Nspire file: "FIFA World Cup 2010". This file can be distributed using TI-Navigator, the TI-Nspire docking station or the teacher/student software. To distribute the file using the Teacher software, use the Tools menu and select the Transfer Tool. Locate the TI-Nspire file on your computer and then start the transfer. Once the file is transferred to the first handheld, unplug the handheld and continue plugging in each student's handheld device. Once all the students have the file, stop the transfer. Note that students can also transfer files from one handheld device to another from within the My Documents folder. Note also that multi-port USB connectors can be used to transfer files to several handhelds at the one time.

This activity requires access to the "FIFA World Cup 2010" TINspire document. This document should be loaded on your device before proceeding.

Once the document is on your handheld, press home and select My Documents. Locate the "FIFA World Cup 2010" document and press enter to open.

Navigate to page 1.3 (shown opposite). Use the arrow keys to scroll across to view the column headings or down to view the data.


## Drawing a boxplot

## Step 1

Press home or ctrl + I and select Add Data \& Statistics to insert a new page.


All of the data points should appear on the screen.


## Step 2

Press tab or use the mouse to highlight list of variables for the horizontal axis. Select age.

A dot plot of the data will appear.

## Step 3

Press menu > Plot Type > Box Plot.

A box plot of the data will appear.


## Step 4

Move the cursor over the box plot to determine the five summary points.

$$
\begin{aligned}
& \mathbf{Q}_{1}-\text { minimum } \\
& \mathbf{Q}_{1}-\text { lower quartile } \\
& \mathbf{Q}_{2}-\text { median } \\
& \mathbf{Q}_{3}-\text { upper quartile } \\
& \mathbf{Q}_{5} \text { - maximum }
\end{aligned}
$$



## Drawing multiple boxplots

## Step 1

Press tab or use the mouse to display the variables for the vertical axis. Select group.


## Step 2

Multiple box plots for the groups will appear. To determine a median for a group, move the mouse and hover over the middle of the box for that group. For example group F has a median age of 28 years.

## Optional

To display a box plot in colour on a CX, place the cursor over the box plot and press ctrl + menu > Color > Fill Color*. Select a colour from the palette.

* On a Clickpad or Touchpad, this command provides a range of grey scale options to select from.


For the remainder of this activity, we will use coloured box plots. In black and white, these will appear in grey scale.


To compare the weight for each group, select weight on the horizontal axis.


To display the box plots vertically, change the vertical axis to age (or weight) and the horizontal axis to group. If the box plots don't automatically change, press menu > Plot Type > Box Plot again.


Note - There are six categories available in the Lists \& Spreadsheet page 1.3. Three are numerical lists (height, weight and age) and three are categorical lists (position, team and group). To draw multiple box plots, select from the numerical list for one axis and select from the categorical list for the other axis.

## Questions

1. Draw a boxplot which represents the weight of all footballers in the FIFA World Cup.
a. What is the median weight?
b. What is the interquartile range for the data?
c. There are a number of outliers (shown as dots) in the data. Which position would you expect the heavier outliers to be (forwards, defenders, midfielders or goalkeepers)?
a. 76 kg
b. $80-72=8 \mathrm{~kg}$
c. Goalkeepers represent the outliers

2. Draw boxplots comparing the height of each group (choose group for the vertical axis and height for the horizontal axis). Colouring the box plots is optional.
a. Which group has the highest median height? What is the highest median height?
b. Which group has the lowest interquartile range? What is the IQR?
c. Which group has the most outliers? How many outliers?
a. Group d, 184 cm
b. Group b, 186-180 $=6 \mathrm{~cm}$
c. Group b, 5 outliers

One reason why this group has the highest median weight is due to two outliers from the Nigerian team ( 95 kg and 101 kg ).

3. Draw boxplots comparing the weight and the positions (choose position for the vertical axis and weight for the horizontal).
a. Which position (defender, forward, goalkeeper or midfielder) has the greatest median weight? What is the median weight?
b. Which two positions appear to be evenly matched?
c. Which position has the lowest interquartile range? What is the IQR?
a. Goalkeeper, 83 kg
b. Forwards and defenders
c. Defenders, $80-73=7 \mathrm{~kg}$

Goalkeepers are generally heavier since they are taller than the average footballer. A tall goalkeeper is able to handle reach the high balls better than a short goalkeeper.

4. Draw boxplots comparing the ages and the positions of footballers (choose position for the vertical axis and age for the horizontal).
a. Which position (forward, midfielder, defender or goalkeeper) has the highest median age? What is the median age?
b. Which position has the lowest median age? What is the lowest median age?
c. Which position has the greatest interquartile range? What is the IQR?
d. Which positions appear to be similar in their distribution of ages?
a. Goalkeepers, 28 years
b. Midfielders and forwards, 26 years
c. Goalkeepers, $31.5-25.5=6$ years
d. Defenders, forwards and midfielders

Goalkeepers are older on average as their fitness requirements are not as demanding as outfield players and they can consequently last longer in their career choice.

5. Draw boxplots comparing the weights and the positions of footballers (choose position for the vertical axis and weight for the horizontal).
a. Which position (forward, midfielder, defender or goalkeeper) has the highest median weight? What is the median weight?
b. Which position has the lowest median weight? What is the lowest median weight?
c. Which position has the lowest interquartile range? What is the IQR?
d. Which positions appear similar in their distribution?
a. Goalkeepers, 83 kg
b. Midfielders, 73 kg
c. Defenders, $80-73=7 \mathrm{~kg}$
d. Defenders and forwards are very similar in their distribution. Defenders range from 62 kg to 95 kg and forwards range from 60 kg to 94 kg .

Goalkeepers are heavier in general since they are taller on average. Tall goalkeepers
 have an obvious advantage over shorter players, especially with high balls.
6. Draw boxplots comparing the ages of the players from each team (choose age for the vertical axis and team for the horizontal)
a. Which team has the lowest median age? What is the lowest median age?
b. Which team has the lowest interquartile range? What is the IQR?
a. Ghana, 23 years
b. Netherlands, $28-26=2$ years

Use the computer view for a less congested view of the teams.


